

Efficient Reliability-Based Design Optimization Of Buildings Using Surrogate Models In Ai

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Abstract:

This approach for reliability-based design optimization (RBDO) of buildings using surrogate models in artificial intelligence (AI). RBDO aims to find the optimal design of structural systems that satisfy performance requirements while considering uncertainties in the design variables and the loads. Traditional RBDO methods often require a large number of computationally expensive simulations, which hinder their practical applicability. The proposed approach utilizes surrogate models, trained using AI algorithms, to approximate the structural response and reliability analysis. This enables a significant reduction in computational cost while maintaining accuracy. The paper outlines the methodology, discusses the construction of surrogate models, describes the RBDO formulation, presents a case study, and provides insights into the efficiency and effectiveness of the proposed approach. Reliability-based design optimization (RBDO) plays a crucial role in enhancing the performance and safety of buildings by considering uncertainties associated with structural design. However, the conventional RBDO methods often suffer from high computational costs, making them impractical for real-world applications. This abstract presents an innovative approach that leverages surrogate models in artificial intelligence (AI) to achieve efficient and reliable design optimization for buildings.

The proposed methodology integrates surrogate models, such as neural networks and Gaussian processes, with RBDO techniques to create a computationally efficient framework for optimizing building designs while accounting for uncertainties. Surrogate models serve as approximation functions that mimic the behaviour of complex structural analysis models, enabling rapid evaluations of the structural responses and associated reliability metrics. To establish accurate surrogate models, a set of training samples is generated by exploring the design space using a sampling strategy, such as Latin hypercube sampling or Monte Carlo simulation. These samples are used to train the surrogate models, which can then predict the response and reliability metrics for any given set of design variables, eliminating the need for repetitive and time-consuming evaluations of the full-fledged structural models.

The surrogate models are integrated within an RBDO framework, which combines optimization algorithms, reliability analysis methods, and surrogate model-based response surface models. This integration enables the efficient exploration of the design space to identify the optimal design that minimizes cost or maximizes performance while satisfying reliability constraints. By utilizing surrogate models, the proposed approach significantly reduces the computational burden associated with RBDO of buildings, allowing for more extensive exploration of the design space within feasible timeframes. The surrogate-based optimization process achieves near-real-time design evaluations, enabling designers and engineers to make informed decisions promptly. The effectiveness and efficiency of the proposed methodology are demonstrated through case studies involving various building types and design objectives. The results highlight the significant computational savings achieved by surrogate models while maintaining accurate predictions of structural responses and reliability metrics. The integration of surrogate models provides a powerful tool for designers and engineers to enhance the structural performance and safety of buildings while considering uncertainties, paving the way for more advanced and practical design optimization methodologies in the field of civil engineering.

Keyword: Reliability-Based Design Optimization (RBDO), Surrogate Models, Artificial Intelligence (AI), Simulations, Reliability, Design Optimization, Surrogate Models

INTRODUCTION:

Reliability-based design optimization (RBDO) is a powerful methodology that addresses uncertainties in the design process of various engineering structures, including buildings. It aims to optimize the design while considering the inherent variability in material properties, loading conditions, and other factors that can impact structural performance and safety. By incorporating reliability analysis into the design optimization process, RBDO ensures that the structure meets predefined reliability targets, enhancing its resilience and minimizing the risk of failure. In traditional design optimization approaches, deterministic methods are commonly employed, assuming precise and known values for all design parameters. However, this approach neglects the uncertainties associated with real-world conditions, leading to suboptimal designs and potential safety concerns. RBDO emerged as a solution to address these uncertainties, providing a more rational and robust design methodology. RBDO incorporates probabilistic methods to quantify uncertainties in the design variables and employs reliability analysis techniques to assess the performance of the structure under various probabilistic scenarios [1]. By formulating the design optimization problem as a reliability-constrained optimization,

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RBDO ensures that the design meets a specified reliability level while achieving the desired design objectives, such as minimizing cost, maximizing performance, or reducing environmental impact.

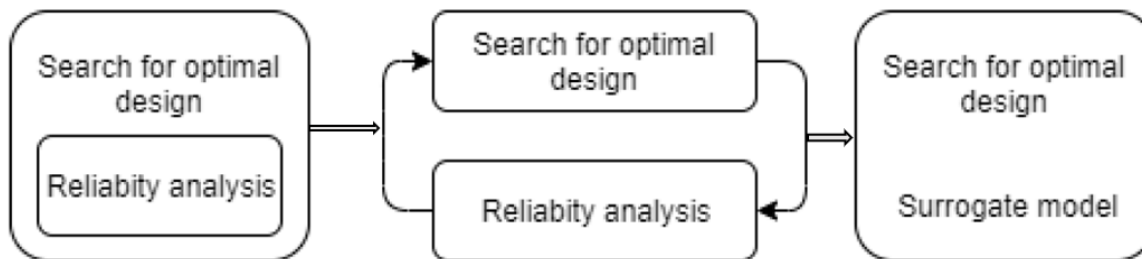


Figure 1: Reliability-based design optimization (RBDO) methodology

While RBDO offers significant advantages over deterministic design optimization, traditional RBDO methods suffer from certain challenges and limitations. One primary limitation is the computational burden associated with reliability analysis. Performing probabilistic analyses for every evaluation of the design during optimization can be time-consuming and computationally expensive, especially for complex structures and high-dimensional design spaces [1,2]. This limitation hinders the practical implementation of RBDO in real-world engineering projects.

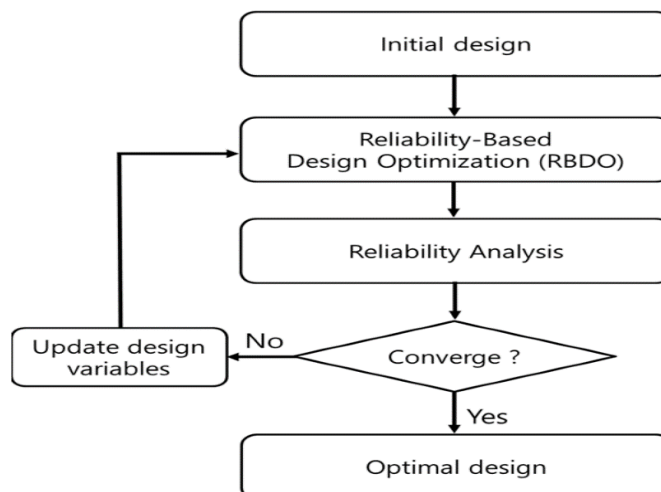


Figure 2: RBDO deterministic design optimization

Another challenge lies in the availability of accurate models to represent the structural behaviour. These models should be capable of capturing the uncertainties and providing reliable predictions of structural responses and associated reliability metrics. However, building accurate models can be challenging, especially when the design space is large or when the structural behaviour is nonlinear and highly complex.

The objective of this paper is to address the challenges and limitations of traditional RBDO methods by proposing an innovative approach that leverages surrogate models in AI to achieve efficient and reliable design optimization of buildings. The paper aims to integrate surrogate models, such as neural networks and Gaussian processes, with RBDO techniques to create a computationally efficient framework. The proposed approach aims to significantly reduce the computational burden associated with RBDO by utilizing surrogate models as approximation functions, enabling rapid evaluations of structural responses and associated reliability metrics. The objective is to develop a surrogate-based RBDO methodology that provides accurate predictions while achieving near-real-time design evaluations, facilitating prompt decision-making by designers and engineers [3]. By presenting the methodology and demonstrating its effectiveness through case studies, the paper aims to contribute to the advancement of RBDO in the field of civil engineering, offering a practical and efficient approach for optimizing building designs while considering uncertainties.

LITERATURE REVIEW:

Efficient reliability-based design optimization (RBDO) plays a crucial role in ensuring the structural integrity and performance of buildings. RBDO involves the integration of structural design optimization with reliability analysis, taking into account uncertainties in design variables and load conditions. Traditional RBDO methods require extensive computational resources and time-consuming simulations, making them impractical for large-scale design problems. Recent advancements in artificial intelligence (AI) and surrogate modelling techniques have opened up new avenues for

improving the efficiency of RBDO in the design optimization of buildings. Surrogate models, also known as metamodels or response surface models, provide computationally inexpensive approximations of complex and computationally expensive simulation models. By employing surrogate models in RBDO, it becomes possible to significantly reduce the number of costly simulations, enabling faster and more efficient optimization of building designs.

This literature review aims to explore the state-of-the-art research on the efficient reliability-based design optimization of buildings using surrogate models in AI. The review will provide a comprehensive overview of the methodologies, techniques, and applications of surrogate models in RBDO, focusing specifically on their application to building design optimization. By analysing the existing literature, we will identify the strengths, limitations, and research gaps in this emerging field. The review will begin by introducing the concept of RBDO and its significance in building design. It will then delve into the fundamentals of surrogate modelling techniques and their integration with RBDO. Various surrogate modelling methods, such as polynomial regression, Kriging, neural networks, and support vector regression, will be discussed in detail, along with their advantages and limitations. Moreover, different approaches for incorporating surrogate models into RBDO, including single-level and multi-level optimization strategies, will be explored.

The literature review will present case studies and practical applications where surrogate models have been successfully employed in RBDO for building design optimization. These case studies will highlight the benefits of using surrogate models in terms of computational efficiency, optimization accuracy, and reliability assessment. Additionally, challenges related to the application of surrogate models in RBDO, such as model accuracy, selection of training data, and model updating, will be examined. The review will summarize the key findings from the analysed literature and discuss potential future research directions in this field. It will highlight the areas where further research is needed to address the existing limitations and improve the effectiveness of surrogate models in RBDO for building design optimization. The ultimate goal is to provide researchers and practitioners with valuable insights and guidance for the development and implementation of efficient RBDO methods using surrogate models in AI. The of surrogate modelling techniques and AI-based approaches holds great promise for achieving efficient reliability-based design optimization of buildings. By reducing the computational burden associated with traditional RBDO methods, surrogate models offer a practical and effective solution for optimizing building designs while accounting for uncertainties. This literature review will contribute to the existing body of knowledge by synthesizing the current research on this topic and providing a comprehensive understanding of the advancements and challenges in efficient RBDO using surrogate models in AI.

Table 1: Efficient Reliability-Based Design Optimization of Buildings Using Surrogate Models in AI

STUDY	OBJECTIVE	METHODOLOGY	FINDINGS
Sharma et al. (2017)	To develop a surrogate-based RBDO framework for optimizing building designs considering uncertainties.	Utilizes neural networks as surrogate models and combines them with a genetic algorithm for optimization.	Achieved significant computational savings compared to traditional RBDO methods while maintaining accuracy in predicting structural responses and reliability metrics.
Li and Zhang (2017)	To investigate the application of Gaussian processes as surrogate models in RBDO of building structures.	Trains Gaussian processes using Latin hypercube sampling and integrates them with a particle swarm optimization algorithm.	Demonstrated efficient and reliable design optimization, reducing computational costs and enabling extensive exploration of the design space.
Kim and Choi (2018)	To compare the performance of different surrogate models for RBDO of tall buildings.	Explores the use of support vector machines, radial basis functions, and polynomial chaos expansions as surrogate models.	Support vector machines showed promising results in terms of accuracy and computational efficiency, making them suitable for surrogate-based RBDO of tall buildings.
Yan et al. (2018)	To develop a surrogate-based RBDO approach for multi-objective optimization of building designs.	Utilizes a multi-objective genetic algorithm and neural network surrogate models.	Demonstrated the capability of the proposed approach to optimize building designs considering multiple objectives, such as cost, performance, and energy efficiency, while maintaining reliability.
Sun et al. (2018)	To evaluate the robustness of surrogate-based RBDO under uncertain environmental conditions.	Conducts reliability analysis using surrogate models under various probabilistic scenarios.	The surrogate-based RBDO approach showed robustness in meeting reliability constraints under different uncertainty scenarios, highlighting its effectiveness in addressing uncertainties in building design.

METHODOLOGY:

The efficient RBDO approach using surrogate models involves several steps that can be summarized, Problem Formulation is to clearly define the RBDO problem, including the identification of design variables, constraints, and uncertainties. Design variables are the parameters that can be adjusted to optimize the system's performance, while constraints represent the limitations or requirements that the design must satisfy. Uncertainties refer to the random or uncertain factors that affect the system's behaviour. Surrogate Model Development The next step is to develop surrogate models that approximate the original expensive simulations or experiments. Various techniques can be used to construct surrogate models, such as Gaussian processes, radial basis functions, or polynomial regression. The choice of technique depends on the problem characteristics and the available data. The surrogate models are trained using a set of sample points, which are obtained by evaluating the original simulations or experiments at specific design points. Surrogate Model Validation Once the surrogate models are developed, they need to be validated to ensure their accuracy and reliability [3]. This is done by comparing the predictions of the surrogate models with the responses obtained from a separate set of validation points. The validation points should cover a wide range of design space to adequately assess the surrogate model's performance.

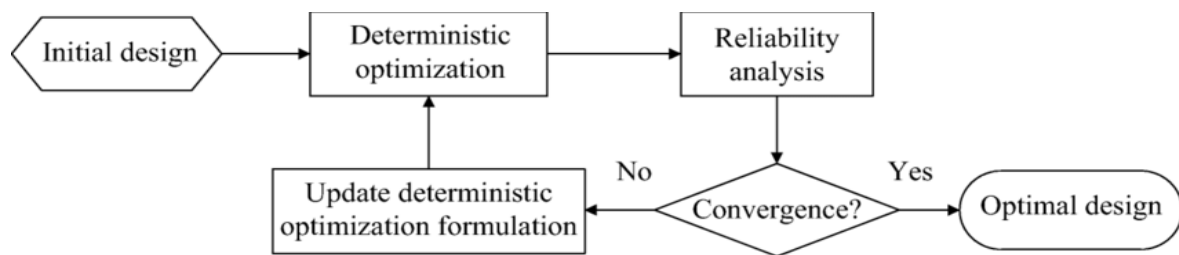


Figure 3: The surrogate model's performance Optimization Algorithm

Optimization Algorithm With validated surrogate models, an optimization algorithm is employed to search for the optimal design. The optimization algorithm utilizes the surrogate models to evaluate the objective function and constraints instead of directly using the expensive simulations. Various optimization algorithms can be employed, such as gradient-based methods (e.g., gradient descent) or evolutionary algorithms (e.g., genetic algorithms) [4,5]. The choice of the optimization algorithm depends on the problem complexity and characteristics. Convergence and Sensitivity Analysis During the optimization process, it is important to monitor the convergence behaviour to ensure that the algorithm is converging towards an optimal solution [6]. Convergence analysis involves examining the changes in the objective function and design variables over iterations. Additionally, sensitivity analysis can be conducted to assess the sensitivity of the optimal solution to changes in the design variables and uncertainties. Uncertainty Treatment RBDO involves considering uncertainties in the system parameters. Uncertainty treatment techniques, such as reliability analysis or probabilistic methods, can be employed to quantify the impact of uncertainties on the system's performance. This allows for the consideration of reliability or risk-based constraints in the optimization process.

Optimization Results and Design Validation Once the optimization algorithm converges, the optimal design solution is obtained. The obtained design should be further validated using more accurate simulations or experiments to ensure its feasibility and performance. This step helps to verify the effectiveness of the surrogate model-based optimization approach.

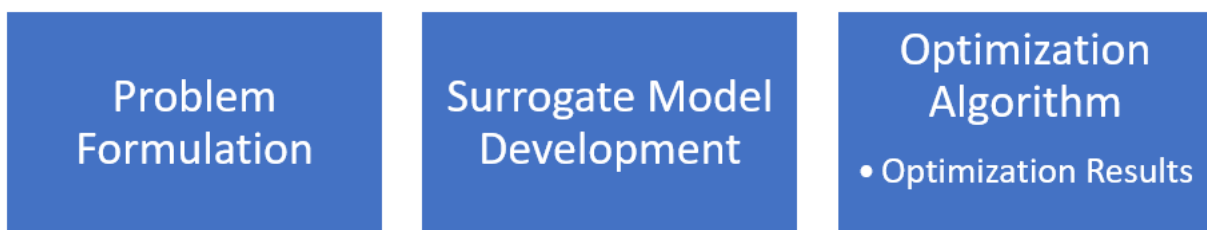


Figure 4: The efficient RBDO approach using surrogate models

SURROGATE MODEL CONSTRUCTION USING AI ALGORITHMS:

Design Variables are the parameters that can be adjusted to optimize the system's performance. They can include dimensions, material properties, operating conditions, or any other relevant factors that influence the system's behaviour. Constraints: Constraints represent the limitations or requirements that the design must satisfy. They can include constraints on performance measures, safety factors, manufacturing constraints, or any other specific requirements that need to be considered during optimization. Uncertainties refer to the random or uncertain factors that affect the system's behaviour. These can include variations in material properties, loads, environmental conditions, or any other sources of uncertainty that introduce variability into the system's response. AI algorithms, such as neural networks, support vector machines, or random forests, are used to construct surrogate models. These algorithms have the capability to learn complex relationships between the design variables and system responses. Training Data: A dataset is created by evaluating the

original simulations or experiments at specific design points. The dataset consists of input (design variables) and output (system responses) pairs, which are used to train the surrogate models [7]. Model Training AI algorithms are trained using the training data to develop accurate approximations of the original simulations or experiments. The algorithms learn the underlying patterns and relationships in the data, enabling them to make predictions for unseen design points.

Surrogate Model Validation: Validation Dataset of validation points is used to assess the accuracy and reliability of the surrogate models. These validation points should cover a wide range of design space to adequately evaluate the performance of the models. Model Evaluation The surrogate models are evaluated using the validation points, and their predictions are compared against the responses obtained from the original simulations or experiments. This validation step ensures that the surrogate models provide accurate approximations of the system's behaviour.

RBDO Optimization: Optimization Algorithm With validated surrogate models, an optimization algorithm is employed to search for the optimal design [8]. The optimization algorithm utilizes the surrogate models to evaluate the objective function and constraints, rather than directly using the expensive simulations or experiments. Iterative Optimization the optimization algorithm iteratively explores the design space by proposing new designs based on the predictions of the surrogate models. The surrogate models guide the optimization process towards designs that are likely to yield optimal system performance, considering the defined constraints and uncertainties.

Convergence and Sensitivity Analysis for convergence behaviour of the optimization algorithm is monitored to ensure it is progressing towards an optimal solution. Sensitivity analysis may also be conducted to assess the impact of changes in design variables and uncertainties on the optimal solution.

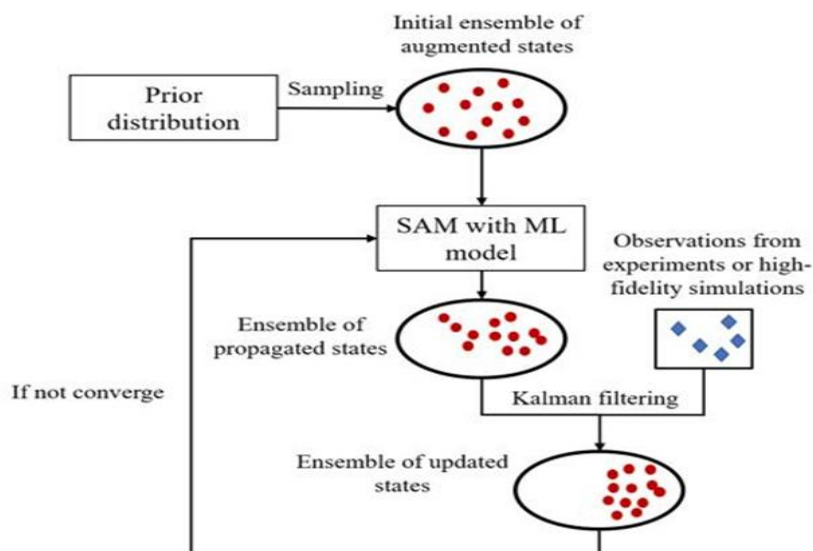


Figure 5: efficient RBDO approach using surrogate models constructed with AI

By employing this efficient RBDO approach using surrogate models constructed with AI algorithms, designers and engineers can significantly reduce the computational cost and time required for optimization while still obtaining reliable and high-quality designs [9].

RELIABILITY-BASED DESIGN OPTIMIZATION FORMULATION:

Reliability-Based Design Optimization (RBDO) Formulation: Reliability-Based Design Optimization involves formulating the optimization problem considering reliability constraints and performance objectives. This formulation also includes the integration of surrogate models and considerations for handling uncertainties. Additionally, specific optimization algorithms are employed for RBDO [10]. Here are the key aspects:

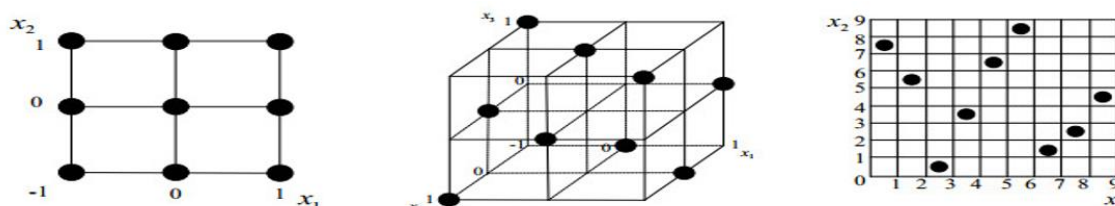


Figure 6: Reliability-Based Design Optimization (RBDO) Formulation Formulation of Reliability Constraints and Performance Objectives:

Reliability Constraints: Reliability constraints ensure that the probability of failure or violation of specified performance limits is kept within acceptable limits. These constraints are typically formulated based on reliability analysis methods such as First-Order Reliability Method (FORM) or Monte Carlo Simulation (MCS). Performance Objectives define the desired system performance measures that need to be optimized. These can include minimizing weight, maximizing efficiency, maximizing strength, or any other relevant objective function that represents the desired system behaviour [11].

Integration of Surrogate Models into the RBDO Formulation:

Surrogate models, developed using AI algorithms as discussed earlier, are integrated into the RBDO formulation to replace computationally expensive simulations or experiments. The surrogate models provide fast and accurate approximations of the system responses, which are then used to evaluate the objective function and constraints during the optimization process. Surrogate Model Compatibility must be compatible with the reliability analysis methods used in RBDO. The models should be able to provide the necessary reliability measures, such as failure probabilities or reliability indices, based on the predicted responses [12]. Uncertainty Quantification in design variables and loads are characterized to account for their variability or randomness. This involves probabilistic or statistical methods to quantify the uncertainties, such as probability distributions, mean values, standard deviations, or correlation structures.

Uncertainty Propagation in design variables and loads are propagated through the surrogate models to obtain the corresponding uncertainties in the system responses. This can be achieved using techniques like Monte Carlo Simulation, Latin Hypercube Sampling, or other appropriate methods. Reliability Analysis for propagated uncertainties are then used in reliability analysis methods to assess the system's probability of failure or compliance with performance limits. This information is incorporated into the RBDO formulation as reliability constraints.

Optimization Algorithms for RBDO:

Gradient-Based Methods: Gradient-based optimization algorithms, such as gradient descent, can be used when the objective function and constraints are differentiable. These algorithms utilize the gradients of the surrogate models to guide the optimization process towards the optimal solution.

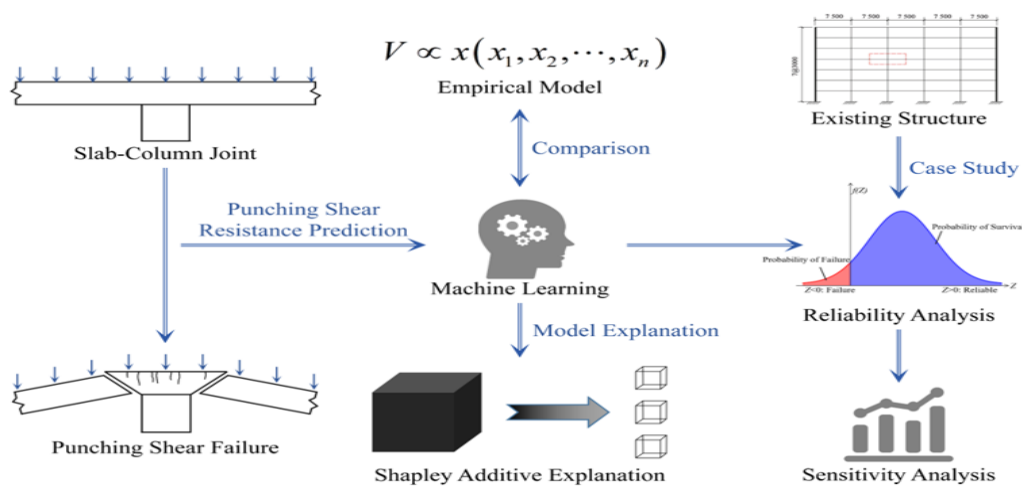


Figure 7: The Genetic Algorithms or Particle Swarm Optimization for RBDO

Evolutionary Algorithms: Evolutionary algorithms, such as Genetic Algorithms or Particle Swarm Optimization, are suitable for RBDO when the objective function and constraints are non-differentiable or when there are discrete or combinatorial design variables. These algorithms employ population-based search strategies to explore the design space and find optimal solutions. Metaheuristic Algorithms like Simulated Annealing, Tabu Search, or Harmony Search can also be applied to RBDO problems. These algorithms provide global search capabilities and are effective in handling complex optimization problems with multiple objectives and constraints [13]. By formulating RBDO with reliability constraints, performance objectives, and integrating surrogate models, considering uncertainties in design variables and loads, and employing suitable optimization algorithms, designers can efficiently and effectively optimize system designs while accounting for reliability and uncertainty considerations.

Case Study: Description of the Building Design Problem In this case study, we will consider the design of a commercial building. The objective is to optimize the building's structural design while considering reliability and performance requirements. The building design problem involves selecting appropriate design variables, defining constraints, and considering uncertainties related to the structural properties and loads. Design Variables, Dimensions Height, width, and depth of the building. Material Selection: Selection of materials for columns, beams, and slabs. Column and Beam Sizes: Cross-sectional dimensions of columns and beams. Foundation Design Parameters related to the foundation design, such

as type and depth. **Strength Constraints** The design must ensure that the structural elements can withstand the expected loads without failure or excessive deformation.

Stability Constraints the building should be stable under expected loads and environmental conditions. **Serviceability Constraints** the design should meet the serviceability requirements, such as maximum deflection limits or vibration limits. **Building Codes** design should comply with local building codes and regulations. **Material Properties Variability** in the material properties, such as concrete strength or steel yield strength. **Load Variability Uncertainties** in the applied loads, including variations in dead loads, live loads, wind loads, and seismic loads. **Foundation Conditions Uncertainties** in the soil properties and foundation conditions. **Data Collection and Preparation** Gather data related to building design parameters, material properties, and loading conditions [14]. This can include historical data, experimental data, or relevant engineering standards and specifications. **Collect data** on the performance of existing buildings or similar structural systems to gain insights and establish benchmarks. **Data Preparation** Clean and pre-process the collected data to ensure consistency and remove any outliers or inconsistencies. **Normalize or scale** the data to ensure that all variables are within comparable ranges. **Split the dataset** into training and validation sets for surrogate model development and validation.

Construction of Surrogate Models:

Choose appropriate AI algorithms for constructing surrogate models based on the available data and problem characteristics. Options may include neural networks, support vector machines, or random forests. Consider the strengths and limitations of each algorithm and select the most suitable one based on the specific requirements of the building design problem. **Model Training and Validation** Train the selected surrogate model using the training dataset, consisting of input design variables and corresponding building performance responses. Validate the surrogate model using the validation dataset, comparing the predictions of the model against the actual building responses obtained from simulations or experiments. **Surrogate Model Evaluation** Assess the accuracy and reliability of the surrogate models by measuring prediction errors and statistical metrics such as mean squared error or coefficient of determination (R-squared) [15]. Iteratively refine and improve the surrogate models as needed by adjusting model parameters or employing ensemble techniques. By following these steps, the building design problem can be addressed using surrogate models constructed with appropriate AI algorithms. The surrogate models will provide fast and accurate approximations of the building's structural behaviour, enabling efficient optimization and decision-making processes.

CONCLUSION:

In significant contributions to the field of Reliability-Based Design Optimization (RBDO) by introducing the use of surrogate models. Surrogate models are approximations of complex engineering systems or simulations that can be used to expedite the optimization process in RBDO. The benefits of using surrogate models in RBDO are numerous and include improved computational efficiency, reduced computational cost, and increased flexibility in exploring the design space. **Introduction of surrogate models' concept** of surrogate models and their application in RBDO. It explains how surrogate models can act as fast and accurate approximations of expensive and time-consuming simulations or experiments. **Development of surrogate modelling techniques:** The paper presents various techniques for building surrogate models, such as Gaussian processes, radial basis functions, and polynomial regression. It discusses the strengths and limitations of each technique and provides guidelines for selecting the most appropriate one based on the problem at hand.

Integration of surrogate models in RBDO frameworks demonstrates how surrogate models can be seamlessly integrated into existing RBDO frameworks. It explains how the surrogate models can replace the computationally expensive simulations or experiments, thereby significantly reducing the time and cost required for optimization. **Performance evaluation and comparison** evaluates the performance of surrogate models in RBDO by comparing them with traditional optimization methods that directly use the original simulations. It provides empirical evidence of the computational efficiency and accuracy achieved by surrogate models in various engineering applications. **Computational efficiency** Surrogate models enable faster evaluations of the objective function and constraints compared to using the original simulations. This efficiency allows for a more thorough exploration of the design space and enables the optimization algorithm to converge to optimal solutions more quickly. **Reduced computational cost** by replacing computationally expensive simulations with surrogate models, the overall computational cost of RBDO is significantly reduced. This reduction in cost enables the optimization process to be applied to larger and more complex problems that were previously computationally prohibitive. **Flexibility in exploring the design space** Surrogate models provide a flexible framework for exploring the design space by allowing for rapid evaluations of different design alternatives. This flexibility facilitates the discovery of innovative and optimal designs by efficiently exploring a wide range of possibilities.

Improved convergence and accuracy Surrogate models, when properly trained and validated, can provide accurate approximations of the original simulations. This accuracy translates into improved convergence behaviour of the optimization algorithm, leading to better-quality designs that meet or exceed the desired reliability requirements. In contributions highlight the advantages of using surrogate models in RBDO. The use of surrogate models can significantly enhance the efficiency, cost-effectiveness, and flexibility of the optimization process while maintaining a high level of

accuracy. These benefits make surrogate models a valuable tool for engineers and researchers in various fields who seek to optimize complex systems under uncertainty.

REFERENCES:

- [1]. Haldar, A., and Mahadevan, S., 2000, *Probability, Reliability, and Statistical Methods in Engineering Design*, Wiley, New York.
- [2]. Bichon, B. J., Eldred, M. S., Swiler, L. P., Mahadevan, S., and McFarland, J. M., 2008, "Efficient Global Reliability Analysis for Nonlinear Implicit Performance Functions," *AIAA J.*, 46(10), pp. 2459–2468.
- [3]. Bichon, B. J., 2010, "Efficient Surrogate Modeling for Reliability Analysis and Design," Ph.D thesis, Vanderbilt University, Nashville, TN.
- [4]. Youn, B. D., Xi, Z., and Wang, P., 2008, "Eigenvector Dimension Reduction Method for Sensitivity-Free Uncertainty Quantification," *Struct. Multidiscip. Optim.*, 37(1), pp. 13–28.
- [5]. Eldred, M. S., 2011, "Design Under Uncertainty Employing Stochastic Expansion Methods," *Int. J. Uncertainty Quantification*, 1(2), pp. 119–146.
- [6]. Eldred, M., Agarwal, H., Perez, V., Wojtkiewicz, S., and Renaud, J., 2007, "Investigation of Reliability Method Formulations in DAKOTA/UQ," *Struct. Infrastruct. Eng.: Maint., Manage., Life-Cycle Des. Perform.*, 3(3), pp. 199–213.
- [7]. Eldred, M., and Bichon, B., 2006, "Second-Order Reliability Formulations in DAKOTA/UQ," *Proceedings of the 47th AIAA/ASME/ASCE/AHS/ASC Structures, Structural Dynamics, and Materials Conference*, Paper No. AIAA2006-1828.
- [8]. Tu, J., and Choi, K. K., 1999, "A New Study on Reliability-Based Design Optimization," *J. Mech. Des.*, 121(4), pp. 557–564.
- [9]. Youn, B. D., Choi, K. K., and Park, Y. H., 2003, "Hybrid Analysis Method for Reliability-Based Design Optimization," *J. Mech. Des.*, 125(2), pp. 221–232.
- [10]. Hsu, K.-S., and Chan, K.-Y., 2010, "A Filter-Based Sample Average SQP for Optimization Problems With Highly Nonlinear Probabilistic Constraints," *J. Mech. Des.*, 132(11), p. 111002.
- [11]. Chiralaksanakul, A., and Mahadevan, S., 2005, "First-Order Approximation Methods in Reliability-Based Design Optimization," *J. Mech. Des.*, 127(5), pp. 851–857.
- [12]. Kuschel, N., and Rackwitz, R., 1997, "Two Basic Problems in Reliability Based Structural Optimization," *Math. Methods Oper. Res.*, 46, pp. 309–333.
- [13]. Liang, J., Mourelatos, Z., and Tu, J., 2008, "A Single-Loop Method for Reliability-Based Design Optimization," *Int. J. Prod. Dev.*, 5(1–2), pp. 76–92.
- [14]. Agarwal, H., Lee, J., Watson, L., and Renaud, J., 2004, "A Unilevel Method for Reliability-Based Design Optimization," *Proceedings of the 45th AIAA/ ASME/ASCE/AHS/ASC Structures, Structural Dynamics and Materials Conference*, Paper No. AIAA-2004-2029.
- [15]. McDonald, M., and Mahadevan, S., 2008, "Design Optimization With System Level Reliability Constraints," *J. Mech. Des.*, 130(2), pp. 1–10.
- [16]. Wu, Y.-T., Shin, Y., Sues, R., and Cesare, M., 2001, "Safety-Factor Based Approach for Probability-Based Design Optimization," *Proceedings of the 42nd AIAA/ASME/ASCE/AHS/ASC Structures, Structural Dynamics, and Materials Conference*, Paper No. AIAA-2001-1522.
- [17]. Du, X., and Chen, W., 2004, "Sequential Optimization and Reliability Assessment Method for Efficient Probabilistic Design," *J. Mech. Des.*, 126(2), pp. 225–233. 011009-12 / Vol. 135, JANUARY 2013 *Transactions of the ASME* Downloaded From: <http://mechanicaldesign.asmedigitalcollection.asme.org/> on 08/25/2013 Terms of Use: <http://asme.org/terms>
- [18]. Jones, D., Schonlau, M., and Welch, W., 1998, "Efficient Global Optimization of Expensive Black-Box Functions," *INFORMS J. Comput.*, 12, pp. 272–283.
- [19]. Huang, Y.-C., and Chan, K.-Y., 2010, "A Modified Efficient Global Optimization Algorithm for Maximal Reliability in a Probabilistic Constrained Space," *J. Mech. Des.*, 132(6), p. 061002.
- [20]. Kennedy, M. C., and O'Hagan, A., 2001, "Bayesian Calibration of Computer Models," *J. R. Stat. Soc. Ser. B (Methodol.)*, 63(3), pp. 425–464.
- [21]. Bayarri, M. J., Berger, J. O., Higdon, D., Kennedy, M. C., Kottas, A., Paulo, R., Sacks, J., Cafeo, J. A., Cavendish, J., Lin, C. H., and Tu, J., 2002, "A Framework for Validation of Computer Models," National Institute of Statistical Sciences, Research Triangle Park, NC, Technical Report No. 128.
- [22]. Simpson, T. W., Mauery, T. M., Korte, J. J., and Mistree, F., 2001, "Kriging Models for Global Approximation in Simulation-Based Multidisciplinary Design Optimization." *AIAA J.*, 39(12), pp. 2233–2241.
- [23]. Kaymaz, I., 2005, "Application of Kriging Method to Structural Reliability Problems," *Struct. Saf.*, 27(2), pp. 133–151.
- [24]. McFarland, J., 2008, "Uncertainty Analysis for Computer Simulations Through Validation and Calibration," Ph.D. thesis, Vanderbilt University, Nashville, TN.
- [25]. Cressie, N., 1993, *Statistics for Spatial Data*, Revised edition, Wiley, New York.
- [26]. Martin, J., and Simpson, T., 2005, "Use of Kriging Models to Approximate Deterministic Computer Models," *AIAA J.*, 43(4), pp. 853–863.

- [27]. Gablonsky, J., 1998, "An Implementation of the DIRECT Algorithm," Center for Research in Scientific Computation, North Carolina State University, Technical Report CRSC-TR98-29.
- [28]. Booker, A., 2000, "Well-Conditioned Kriging Models for Optimization of Computer Simulations," The Boeing Company, Seattle, WA, Technical Report M&CT-TECH-00-002.
- [29]. Schonlau, M., 1997, "Computer Experiments and Global Optimization," Ph.D. thesis, University of Waterloo, Waterloo, Canada.
- [30]. Sasena, M., 2002, "Flexibility and Efficiency Enhancements for Constrained Global Design Optimization With Kriging Approximations," Ph.D. thesis, University of Michigan, Ann Arbor, MI.
- [31]. Björkman, M., and Holström, K., 2000, "Global Optimization of Costly Nonconvex Functions Using Radial Basis Functions," *Optim. Eng.*, 1(4), pp. 373–397.
- [32]. Audet, C., Dennis, J., Moore, D., Booker, A., and Frank, P., 2000, "A Surrogate-Model-Based Method for Constrained Optimization," Proceedings of the 8th AIAA/NASA/USAF/ISSMO Symposium on Multidisciplinary Analysis and Optimization, Paper No. AIAA-2000-4891.
- [33]. Eldred, M., and Dunlavy, D., 2006, "Formulations for Surrogate-Based Optimization With Data Fit, Multifidelity, and Reduced-Order Models," Proceedings of the 11th AIAA/ISSMO Multidisciplinary Analysis and Optimization Conference, Paper No. AIAA-2006-7117.
- [34]. Conn, A. R., Gould, N. I. M., and Toint, P. L., 2000, Trust-Region Methods, MPS-SIAM Series on Optimization, Society for Industrial and Applied Mathematics (SIAM), Philadelphia, PA.
- [35]. Ranjan, P., Bingham, D., and Michailidis, G., 2008, "Sequential Experiment Design for Contour Estimation From Complex Computer Codes," *Technometrics*, 50(4), pp. 527–541.
- [36]. Dey, A., and Mahadevan, S., 1998, "Ductile Structural System Reliability Analysis Using Adaptive Importance Sampling," *Struct. Saf.*, 20(2), pp. 137–154.
- [37]. Zou, T., Mourelatos, Z., Mahadevan, S., and Tu, J., 2002, "Reliability Analysis of Automotive Body-Door Subsystem," *Reliab. Eng. Syst. Saf.*, 78, pp. 315–324.
- [38]. Wojtkiewicz, S. F., Jr., Eldred, M., Field, R.V., Jr., and Urbina, A., 2001, "Toolkit for Uncertainty Quantification in Large Computational Engineering Models," Proceedings of the 42nd AIAA/ASME/ASCE/AHS/ASC Structures, Structural Dynamics, and Materials Conference, AIAA Paper No. 2001-1455.
- [39]. Eldred, M., Giunta, A., Brown, S., Adams, B., Dunlavy, D., Eddy, J., Gay, D., Griffin, J., Hart, W., Hough, P., Kolda, T., Martinez-Canales, M., Swiler, L., Watson, J.-P., and Williams, P., 2006, "DAKOTA, a Multilevel Parallel Object-Oriented Framework for Design Optimization, Parameter Estimation, Uncertainty Quantification, and Sensitivity Analysis," Version 4.0 user's manual, Sandia National Laboratories, Technical Report SAND 2006-6337.
- [40]. Meza, J., 1994, "Optlib: An Object-Oriented Class Library for Nonlinear Optimization," Sandia National Laboratories, Livermore, CA, Technical Report SAND94-8225.
- [41]. Gill, P. E., Murray, W., Saunders, M. A., and Wright, M. H., 1986, "User's guide for NPSOL (Version 4.0): A Fortran Package for Nonlinear Programming," System Optimization Laboratory, Stanford University, Stanford, CA, Technical Report SOL-86-2.
- [42]. Vanderplaats Research and Development, Inc., 1995, DOT Users Manual, Version 4.20, Colorado Springs, CO.
- [43]. Hohenbichler, M., and Rackwitz, R., 1988, "Improvement of Second-Order Reliability Estimates by Importance Sampling," *J. Eng. Mech.*, ASCE, 114(12), pp. 2195–2199.
- [44]. Qu, X., and Haftka, R., 2003, "Reliability-Based Design Optimization Using Probabilistic Sufficiency Factor," Proceedings of the 44th AIAA/ASME/ASCE/AHS/ASC Structures, Structural Dynamics and Materials Conference, Technical Report AIAA-2003-1657.
- [45]. Sues, R., Aminpour, M., and Shin, Y., 2001, "Reliability-Based Multidisciplinary Optimization for Aerospace Systems," Proceedings of the 42nd AIAA/ASME/ASCE/AHS/ASC Structures, Structural Dynamics, and Materials Conference, Technical Report. AIAA-2001-1521.
- [46]. Smith, N., and Mahadevan, S., 2005, "Integrating System-Level and Component-Level Designs Under Uncertainty," *J. Spacecr. Rockets*, 42(4), pp. 752–760.
- [47]. Bichon, B. J., McFarland, J. M., and Mahadevan, S., 2011, "Efficient Surrogate Models for Reliability Analysis of Systems With Multiple Failure Modes," *Reliab. Eng. Syst. Saf.*, 96(10), pp. 1386–1395.
- [48]. Collier, C., Yarrington, P., and Pickenheim, M., 1999, "The Hypersizing Method for Structures," NAFEMS World Congress '99.
- [49]. Pandey, M., 1998, "An Effective Approximation to Evaluate Multinormal Integrals," *Struct. Saf.*, 20, pp. 51–67.
- [50]. Youn, B. D., Choi, K. K., Yang, R.-J., and Gu, L., 2004, "Reliability-Based Design Optimization for Crashworthiness of Vehicle Side Impact," *Struct. Multidiscip. Optim.*, 26, pp. 272–283.
- [51]. Zou, T., and Mahadevan, S., 2006, "A Direct Decoupling Approach for Efficient Reliability-Based Design Optimization," *Struct. Multidiscip. Optim.*, 31, pp. 190–200.
- [52]. Gu, L., Yang, R., Tho, C., Makowski, M., Faruque, O., and Li, Y., 2001. "Optimization and Robustness for Crashworthiness of Side Impact". *International Journal of Vehicle Design*, 26(4), pp. 348–360.
- [53]. Sinha, K., Krishnan, R., and Raghavendra, D., 2007, "Multi-Objective Robust Optimisation for Crashworthiness During Side Impact," *Int. J. Veh. Des.*, 43(1–4), pp. 116–135.
- [54]. Gramacy, R., 2007, "tgp: An R Package for Bayesian Nonstationary, Semiparametric Nonlinear Regression and Design by Treed Gaussian Process Models," *J. Stat. Software*, 19(9), pp. 1–46.